Monetary Economics

Lecture 4: the basic new Keynesian model, part one

Chris Edmond

 $2nd \ Semester \ 2014$

This class

- Imperfect competition in the goods market
 - **1-** household demand for differentiated products
 - **2-** static price-setting by monopolistically competitive firms
 - **3-** general equilibrium example
- Reading: Gali (2008), chapter 3 sections 3.0–3.1 and appendix 3.1

Monopolistic competition

- Many differentiated products or varieties
- Firms have market power if products are not perfect substitutes

 \Rightarrow if so, price > marginal cost (markup pricing)

• But no genuine strategic interactions between firms

Household demand for differentiated products

• CES utility from differentiated products on interval [0, 1]

$$C \equiv \left(\int_0^1 C(j)^{\frac{\varepsilon - 1}{\varepsilon}} \, dj \right)^{\frac{\varepsilon}{\varepsilon - 1}}, \qquad \varepsilon > 1$$

Love-of-variety: utility is concave in C(j) (since $0 < \frac{\varepsilon - 1}{\varepsilon} < 1$)

• Static budget constraint

$$\int_0^1 P(j)C(j)\,dj \le Z$$

for some given nominal income Z > 0 (exogenous, for now)

Household demand for differentiated products

• Lagrangian with multiplier λ

$$L = \left(\int_0^1 C(j)^{\frac{\varepsilon-1}{\varepsilon}} dj\right)^{\frac{\varepsilon}{\varepsilon-1}} + \lambda \left(Z - \int_0^1 P(j)C(j) dj\right)$$

• First order conditions

$$C(j)$$
 : $C^{\frac{1}{\varepsilon}} C(j)^{-\frac{1}{\varepsilon}} = \lambda P(j)$

These are for every $j \in [0, 1]$

• Marginal rates of substitution equal to price ratio for any j, k

$$\left(\frac{C(j)}{C(k)}\right)^{-\frac{1}{\varepsilon}} = \frac{P(j)}{P(k)}$$

 $\varepsilon\,$ is (constant) elasticity of substitution between products $(\varepsilon>1)$

Ideal price index

• Aggregate the first order conditions over $j \in [0, 1]$ to characterize multiplier λ . Gives

 $C = \lambda \, Z$

• <u>Define</u> *ideal price index* P such that

 $PC \equiv Z \Leftrightarrow \lambda = 1/P$

• First order conditions

$$C(j) = \left(\frac{P(j)}{P}\right)^{-\varepsilon} C \qquad (\varepsilon > 1)$$

Solution for ideal price index

$$P = \left(\int_0^1 P(j)^{1-\varepsilon} dj\right)^{\frac{1}{1-\varepsilon}}$$

Firms: nominal costs

- Nominal cost function $\Psi(Y)$ to produce Y (total variable costs)
- For example, labor costs WN with production function $Y = AN^{1-\alpha}$ implies nominal cost

$$\Psi(Y) = W\left(\frac{Y}{A}\right)^{\frac{1}{1-\alpha}}$$

and nominal marginal cost

$$\Psi'(Y) = \frac{1}{1-\alpha} \frac{W}{A} \left(\frac{Y}{A}\right)^{\frac{\alpha}{1-\alpha}}$$

Firms: static price setting

• Nominal profits for firm j

 $P(j)Y(j) - \Psi(Y(j))$

- Maximize profits by choice of P(j) taking *demand curve* for C(j) = Y(j) as given
- First order condition characterizes optimal price

$$P(j) = \frac{\varepsilon}{\varepsilon - 1} \Psi' \left(\left(\frac{P(j)}{P} \right)^{-\varepsilon} C \right)$$

• Constant markup $\frac{\varepsilon}{\varepsilon - 1} > 1$ over marginal cost

General equilibrium example: households

• Household preferences over *aggregate consumption* and labor supply

$$U(C,N) = \frac{C^{1-\sigma}}{1-\sigma} - \frac{N^{1+\varphi}}{1+\varphi} \quad \text{and} \quad C \equiv \left(\int_0^1 C(j)^{\frac{\varepsilon-1}{\varepsilon}} dj\right)^{\frac{\varepsilon}{\varepsilon-1}}$$

• Budget constraint

$$PC = WN - T$$

where

$$PC = \int_0^1 P(j)C(j)\,dj$$

• First order conditions

$$C(j) = \left(\frac{P(j)}{P}\right)^{-\varepsilon} C \text{ and } N^{\varphi}C^{\sigma} = \frac{W}{P}$$

General equilibrium example: firms

- Constant returns Y(j) = A(j)N(j) (does this imply zero profits?)
- Price for j'th firm

$$P(j) = \frac{\varepsilon}{\varepsilon - 1} \frac{W}{A(j)}$$

- Equilibrium
 - **1-** demand equals supply for each product j

$$C(j) = Y(j)$$

2- demand for labor equals supply of labor

$$N = \int_0^1 N(j) \, dj$$

Aggregation

• Products not perfect substitutes, so <u>define</u> aggregate output

$$Y \equiv \left(\int_0^1 Y(j)^{\frac{\varepsilon-1}{\varepsilon}} dj\right)^{\frac{\varepsilon}{\varepsilon-1}}$$

Implies

$$Y = C$$

• Now <u>define</u> aggregate productivity index by

$$A \equiv \frac{Y}{N}$$

• Can show that solution for A is

$$A = \left(\int_0^1 A(j)^{\varepsilon - 1} \, dj\right)^{\frac{1}{\varepsilon - 1}}$$

General equilibrium: solving the model

• So price index implied by individual prices

$$P = \left(\int_0^1 P(j)^{1-\varepsilon} dj\right)^{\frac{1}{1-\varepsilon}} = \frac{\varepsilon}{\varepsilon - 1} \left(\int_0^1 A(j)^{\varepsilon - 1} dj\right)^{\frac{1}{1-\varepsilon}} W$$

• Real wage

$$\frac{W}{P} = \frac{\varepsilon - 1}{\varepsilon} \left(\int_0^1 A(j)^{\varepsilon - 1} \, dj \right)^{\frac{1}{\varepsilon - 1}} = \frac{\varepsilon - 1}{\varepsilon} \, A(j)^{\varepsilon - 1} \, dj$$

General equilibrium: solving the model

• Two equations in two unknowns C, N for given aggregate productivity index A

$$C = Y = A N$$

and

$$N^{\varphi}C^{\sigma} = \frac{W}{P} = \frac{\varepsilon - 1}{\varepsilon}A$$

• Markup distortion reduces C, N relative to efficient allocation (planner's solution)

Household intertemporal problem

• Household preferences over *aggregate consumption* and labor supply

$$U(C_t, N_t), \qquad C_t \equiv \left(\int_0^1 C_t(j)^{\frac{\varepsilon-1}{\varepsilon}} dj\right)^{\frac{\varepsilon}{\varepsilon-1}}$$

• Intertemporal preferences

$$\mathbb{E}_0\left\{\sum_{t=0}^\infty \beta^t U(C_t, N_t)\right\}$$

• Flow budget constraint at every date and state

$$P_t C_t + Q_t B_t \le B_{t-1} + W_t N_t - T_t$$

where

$$P_t C_t = \int_0^1 P_t(j) C_t(j) \, dj$$

Household first order conditions

• Differentiated products

$$C_t(j) = \left(\frac{P_t(j)}{P_t}\right)^{-\varepsilon} C_t$$

• Labor supply

$$-\frac{U_{n,t}}{U_{c,t}} = \frac{W_t}{P_t}$$

• Intertemporal consumption Euler equation

$$Q_t = \mathbb{E}_t \left\{ \beta \frac{U_{c,t+1}}{U_{c,t}} \frac{P_t}{P_{t+1}} \right\}$$

Next class

- The basic new Keynesian model, part two
 - dynamic price setting with sticky prices
- Reading: Gali (2008), chapter 3 sections 3.2 and appendix 3.2–3.3