

Advanced Macroeconomics Tutorial #5

Monopolistic competition, markups, and profits. Suppose a final good Y is produced by *perfectly competitive* firms using a CES bundle of intermediate goods

$$Y = \left(\int_0^N y(i)^{\frac{\theta-1}{\theta}} di \right)^{\frac{\theta}{\theta-1}}, \quad \theta > 1$$

The final good firms buy intermediate goods at prices $p(i)$ from intermediate producers $i \in [0, N]$. The intermediate producers are *monopolistically competitive* and choose prices $p(i)$ and output $y(i)$ to maximize profits understanding their market power.

Suppose intermediate producers need only labor to produce and have production function

$$y(i) = Al(i), \quad A > 0$$

and take the wage rate W as given. There is a fixed (inelastic) supply of labor $L > 0$.

(a) Let $C(y)$ denote the cost function for each intermediate producer. Show that $C(y)$ is linear

$$C(y) = cy, \quad c > 0$$

and derive a formula for the marginal cost c in terms of the wage W and other parameters.

(b) Show that the optimal price chosen by each producer is given by

$$p = \mu c$$

where $\mu > 1$ is the (gross) markup over marginal cost. Solve for the markup μ .

Now consider a symmetric equilibrium with $y(i) = y$, $p(i) = p$ etc for all $i \in [0, N]$.

(c) Solve for a symmetric equilibrium. In particular, solve for the equilibrium wage W and equilibrium output Y .

(d) Let $s_L = WL/Y$ denote the labor share and s_Π denote the profit share. Solve for s_L and s_Π . Do higher markups increase the profit share? Explain.

Now suppose that to operate each intermediate producer must pay a *fixed cost* $f > 0$ in units of labor. That is, to produce y units of output the producer needs $\ell(y) \equiv f + y/A$ units of labor. Suppose also that there is an unlimited number of potential entrants and that firms enter if they are willing to pay this fixed cost f .

(e) Solve for the equilibrium number of producers N in terms of the fixed cost f and other parameters. Give intuition for your result.